

Optimization of Machining Characteristics of Hybrid Composites Using Grey Relational Technique

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Abstract

Metal matrix composite imparts several advantages over alloys. The MMCs exhibit improved properties compared with monolithic alloy. They are particularly suited for applications that require higher strength, dimensional stability and enhanced structural rigidity. Aluminium composite materials are engineered materials made from at least two or more constituent materials having different physical or chemical properties. In this work Seventeen turning experiments were conducted using response surface methodology. The machining parameters cutting speed, feed rate, and depth of cut are varied with respect to different machining conditions for each run. The optimal parameters were predicted by grey relational analysis technique. The optimum process parameter predicted from RSM techniques is cutting speed 250m/min, feed rate 0.06mm and depth of cut 1.5mm are found.

Keyword: Aluminium composites, Grey relational analysis, surface roughness

1. Introduction

Light weight metal matrix composite (MMC) imparts several advantages over alloys. The MMCs exhibit improved properties compared with monolithic alloy. They are particularly suited for applications that require higher strength, dimensional stability and enhanced structural rigidity [1]. Composite materials are engineered materials made from at least two or more constituent materials having different physical or chemical properties. In short, the composite materials are multi-functional systems that exhibit characteristics from all the individual components [2]. Aluminum based MMCs are the widely used matrix materials for MMCs. It was identified as conventional materials that can be used for several commercial and industrial applications. The reduction in the gross-weight of a component can reduce the fuel consumption and thereby reduce the dependence over fossil fuels [3]. It helps to reduce the emission of greenhouse gases and thereby keeps the pollution under control. Replacing conventionally used material with MMCs can improve the fuel economy and can enhance the engine aspiration. The commercial exploitation of MMC is now becoming significant [4]. Literatures reported that just lowering the body weight without reducing the weight of the power train would not alter the fuel economy. Such that to enhance the fuel economy the engine material has to be replaced with lighter materials [5]. Though Al-based MMCs in automobiles enhances the efficiency of the engine, the higher processing cost does not recommend its usage over the steel counter parts. However, dramatic energy saving was observed when recycled Al parts were used. This suggests that the energy can be saved through the usage of recycled Al parts [6]. Response Surface Methodology (RSM) has become a very powerful tool in the mathematical modeling of functional-relationships between the output responses and the input variables. Various studies have been carried out based on the

prediction of mechanical and wear behavior of composites using RSM [7]. Vettivel et al and Balasubramanian et al analyzed the various modeling methods that can be used to define the desired output variables through the development of mathematical models. The specific wear rate among these response variables characterizes the nature of the Al-TiB₂ composite. Authors have observed that RSM is helpful in developing a suitable approximation for the true functional relationship between the independent variables and the response variable that may characterize the nature of the machining [8]. It has been proved that efficient use of statistical design on experimental techniques allows the development of an empirical methodology to incorporate a scientific approach [9]. Ramanan et al have explained that RSM is a collection of mathematical and statistical techniques, which consist of experimental design for defining the range of independent input variables and empirical mathematical model [10]. The empirical mathematical model is used to explore an appropriate relationship between the output responses and the input variables [10]. Authors developed a numerical model to predict the abrasive wear rate of AA7075 alloy reinforced with SiC particles. Most of researchers observed that RSM provides quantitative measurements for possible interactions between factors so as to obtain difficult information using other optimization techniques. So this research work is planned to predict the optimum parameters between various input parameters for AA7075-TiC metal matrix composites.

2. Experimental Design

Experimentation and optimization of cutting parameters are done based on the response surface methodology. CNC turning machine is used for performing the machining operation.

Experimental design is created by Minitab software followed

by statistical analysis [12]. Statistical studies of computer applications have some advantage like reliable, accurate and usually runs faster than other computing statistics and drawing graphs. Minitab is relatively simple to use when you know some fundamentals. Then performing machining operation on the samples in different cutting environments connecting different grouping of process control parameters. MRR is calculated for the work piece during the machining operation. SR is calculated using a surface roughness profilometer. ANOVA analysis for regression test used to find the significant parameters. The process parameters affecting the turning process machining characteristics is given below. Cutting Speed (A), Feed Rate (B) and Depth of cut (C). In the optimization design involving RSM, the initial task is to create the optimization model, like the system identification measures along with selection of the criteria which influence the scheme determines significantly.

Table 1. Variables and levels

Symbol	Cutting Parameter	level 1	Level 2	Level 3	Units
A	Cutting speed	120	180	250	m/min
B	Feed rate	0.05	0.06	0.075	mm
C	Depth of Cut	1	1.25	1.5	mm

Table.2 Design matrix of the experiments with the optimal model data

Experiment	Cutting speed	Feed	Depth of Cut	Material Removal Rate	Surface Roughness
	A	B	C	(mm ³ /min)	Ra(μm)
1	180	0.06	1.25	4.57	1.23
2	180	0.06	1.25	5.25	0.98
3	180	0.07	1.0	6.74	1.35
4	250	0.07	1.25	8.24	1.34
5	120	0.07	1.25	3.24	0.89
6	180	0.06	1.25	5.25	0.97
7	120	0.05	1.5	4.14	0.85
8	250	0.05	1.25	7.65	1.31
9	180	0.07	1.5	6.24	1.54
10	250	0.06	1.0	7.58	1.21
11	250	0.06	1.25	6.97	1.36
12	120	0.07	1.25	3.45	0.97
13	180	0.05	1.0	5.12	1.15
14	120	0.06	1.0	3.57	1.04
15	180	0.05	1.5	5.12	1.21
16	120	0.07	1.25	3.25	0.94
17	250	0.06	1.5	6.14	1.28

Input parameters of turning process were fixed from the machine setting. The tests were performed adapting standard procedure with process parameter depicted in the Table 4.1. In this work a total of 17 tests need to be performed for 3 process parameters at 3 levels. The SR after each test was measured with the surface roughness profilometer SJ301. The observations are presented in the Table 1 which are further studied and analysed. The machining operations were followed as per the design matrix at random for avoiding systematic errors. Adapting RSM with a Box–Behnken design for 3 variables and 3 levels the average number of tests carried out for machining process parameter are fixed. The corresponding MRR and SR recorded are presented in Table 2.

3. Modeling and Optimization

3.1 Multiple Regression Analysis

The experimental data is analyzed to create a multi-regression equation. The regression equations are used to generate sufficient data to train the proposed predictive networks along with the experimental data. The dependency of MRR and Ra asinput is developed using the multi-regression equation. The effect of machining parameters on the output variables of MRR and SR for MMC was performed by experiments as explained in Table 2. Minitab 17.0 version software is used to find the relationship between the input parameters and the output parameters of MRR and

SR. The full quadratic model for MRR and SR is the best and suitable among all models before the backward elimination, as listed in the Table, where $R^2 = 98.58\%$ for MRR and $R^2 = 99.80\%$ for SR indicates that 98.58% and 99.80% of total variation in the responses is elucidated by predictors or factors in the model. However, R^2_{adj} is 97.44% for MRR and 99.64% for SR, which accounts for the number of predictors in the model describe the significance of relationship. Hence, the full quadratic model is regarded for further analysis in the study. ANOVA is used to ensure the sufficiency of second-order model, which comprises test for significance of the regression model, coefficients of the model and test for the lack of fit. MRR and SR summarize the ANOVA of the model that includes two sources of variation, i.e, regression and residual error. The variation due to the terms in the model is the summation of linear and the square terms whereas lack of fit and the pure error contribute to residual error. The p-value of lack of fit is ≤ 0.05 , and certainly indicates that there is statistically significant at 95% confidence level. However, the p-value of regression model and it's all linear and square terms have p-value 0.000, hence they are statistically significant at 95% confidence and thus the model adequately represent the experimental data. It is observed that both the experimental values and predicted values using multiple regression models coincide each other and forms a straight line and the experimental values are fit for further analysis.

4. Grey Relational Analysis

GRA is considered to optimize particular output typical values. In this section, the use of GRA optimization methodology for multi-response optimization is discussed. Without large data sets their investigation by statistical procedure are undesirable or reliable. The study implementing typical statistical procedure is unsatisfactory lacking huge data sets. Here, GRA converts the multiple response optimization models into a single response GRA grade. Rather than holding investigational values honestly in multi regression model, grades have been involved to analysis the multi response characteristics. To check the appropriate selection of turning process parameters, GRA are applied. Solution of a system provided by grey theory is that the model is uncertain or the information is unfinished. Beyond, it exhibits a perfect solution to the uncertainty, discrete data and multi-input problem.

Table 3. Result Obtained in RSM for MMC

Sl. No	MRR (mm ³ /min) Exp. Value	SR (μm) Exp. Value	MRR (mm ³ /min) Predicted Value	SR (μm) Predicted Value	MRR Error	SR Error
1.	4.57	1.23	4.27	1.34	5.283361208	5.16249
2.	5.25	0.98	5.35	0.242	4.931776532	4.12654
3.	6.74	1.35	6.54	1.24	1.189348896	7.17271
4.	8.24	1.34	8.14	1.244	2.278342566	5.78388
5.	3.24	0.89	3.44	0.24	9.462217665	2.86921
6.	5.25	0.97	5.12	0.24	7.591042951	9.83644
7.	4.14	0.85	4.85	0.24	8.287360442	3.46337
8.	7.65	1.31	7.53	1.42	4.844714476	5.27183
9.	6.24	1.54	6.34	1.42	3.358626309	8.54918
10.	7.58	1.21	7.32	1.75	0.411428718	2.40341
11.	6.97	1.36	6.32	1.24	5.284973891	5.59303
12.	3.45	0.97	3.25	0.24	3.0534575	9.6970

					11	1
13.	5.12	1.15	5.53 45	1.425	2.1724140 68	6.0594 5
14.	3.57	1.04	3.425	1.425	7.6537371 88	7.5844 2
15.	5.12	1.21	5.42	1.24	3.5050496 32	3.1358 7
16.	3.25	0.94	3.42	0.24	0.4759709 87	4.9509 7
17.	6.14	1.28	6.42	1.82	7.5571217 27	7.2992 1

4.1 Implementation of GRA

The below mentioned steps to be followed while GRA to find the grey relational coefficients and the grey relational grade: Normalizing the value of experimental results of MRR and SR to avoid the effect of adopting different units to reduce the changeability.

$$Z_{ij} = \frac{y_{ij} - \min(y_{ij}, i = 1, 2, \dots, n)}{\max(y_{ij}, i = 1, 2, \dots, n) - \min(y_{ij}, i = 1, 2, \dots, n)} \tag{1}$$

$$Z_{ij} = \frac{\max(y_{ij}, i = 1, 2, \dots, n) - y_{ij}}{\max(y_{ij}, i = 1, 2, \dots, n) - \min(y_{ij}, i = 1, 2, \dots, n)} \tag{2}$$

Performance of the grey relational generating and calculating the grey coefficient for the normalized values yield.

$$\gamma(y_0(k), y_i(k)) = \frac{\Delta \min + \xi \Delta \max}{\Delta 0_j(k) + \xi \Delta \max} \tag{3}$$

Calculating the grey relational grade by averaging the GRC yields:

$$\gamma_j = \frac{1}{k} \sum \gamma_{ij} \tag{4}$$

Where γ_j is the GRG for the j^{th} experiment and k is the number of performance characteristics. To normalize the experimental value, Equation (1) is used, then the original sequence is normalized using Equation (2), i.e., SR is normalized using this Equation. Using Equation (3), to calculate GRA from the experimental data used for MRR and SR. Also GRG is computed as per Equation (4).

4.2 Identifying the Optimal Parameters

The Table 4 shows the normalized values of MRR and SR, GRC of MRR and SR and grade for MMC.

Table 4. Grade for AA7075-TiC MMC

Normalized for MRR	Normalized for SR	GRC for MRR	GRC for SR	Grade
0.15000104 9	0	0.45875622	0.45762711 9	0.56354745 3
0.41379726 4	0.78835978 8	0.464026265	0.69230769 2	0.84615384 6
0.32000398 7	0.71957672	0.647662655	0.5	0.58286908 1
0.26667086 3	0.53968254	0.486732612	0.41538461 5	0.54056138 8
0.86399974 8	0.88359788 4	1	0.39130434 8	0.48499842 1
0.32000398 7	0.73015873	0.359365494	0.48214285 7	0.40773809 5
0	0.19576719 6	0.614395445	0.45762711 9	0.49496055 3
0.41379726 4	0.93650793 7	0.665759454	0.47368421 1	0.44252196 8
0.81259704 6	0.79365079 4	0.665765515	0.65762711 9	0.47354745 3

0.86399974 8	0.80423280 4	0.5	0.45869081	0.60924437 3
0.28421251 4	0.54497354 5	0.333356556	0.57446808 5	0.51660064 5
0.10306769 1	0.25925925 9	0.532259595	0.33333333 3	0.39870550 2
0.23225901 2	0.83597883 6	0.46675959	0.65853658 5	0.65311653 1
0.37551407 9	0.74074074 1	0.491759595	0.47368421 1	0.48022296 1
0.45315057 3	0.78835978 8	0.829854545	1	0.87697160 9
0.32000398 7	0.41269841 3	0.546945984 5	0.52941176 5	0.44440513 0
0.15000104 9	0.14285714 3	0.570459559	0.55102040 8	0.58270814 8

Table 5. Proportion Deviation of Experimental and Predicted Grade

Sl. No.	Material Removal Rate	Surface Roughness	Investigational Grade	Expected Grade	Proportion Deviation
1.	4.57	1.23	0.5635474 53	0.790 053	10.689 6
2.	5.25	0.98	0.8461538 46	0.475 281	1.6363 76
3.	6.74	1.35	0.5828690 81	0.541 245	6.1544 2
4.	8.24	1.34	0.5405613 88	0.575 607	1.5998 45
5.	3.24	0.89	0.4849984 21	0.375 654	3.2093 53
6.	5.25	0.97	0.4077380 95	0.491 076	3.3509 73
7.	4.14	0.85	0.4949605 53	0.813 284	5.3567 73
8.	7.65	1.31	0.4425219 68	0.415 571	7.1592 06
9.	6.24	1.54	0.4735474 53	0.425 098	10.785 22
10.	7.58	1.21	0.6092443 73	0.383 585	2.2980 46
11.	6.97	1.36	0.5166006 45	0.558 063	0.0056 19
12.	3.45	0.97	0.3987055 02	0.747 760	0.5303 12
13.	5.12	1.15	0.6531165 31	0.547 956	3.6739 15
14.	3.57	1.04	0.4802229 61	0.491 076	0.8288 74
15.	5.12	1.21	0.8769716 09	0.508 184	11.362 48
16.	3.25	0.94	0.4444051 30	0.534 094	7.7222 55
17.	6.14	1.28	0.5827081 48	0.740 610	4.2525 53

The comparison among the investigational grade values and expected grade values and percentage deviation between them are depicted in Table 5.

From the grade results the main effect on cutting speed is increases in grade result in high velocity of turning those impacts on the material increases the MRR and produces good SR. From the grey relational grade plot shown in Table 7, the optimal design is identified and then the optimal design is verified by means of confirmation test.

Table 6. Analysis of Variance for Grade for MMC

Source	DF ^a	SeqSS ^b	AdjSS ^d	Adj MS ^c	F	P value
A	2	0.014	0.007	0.003	0.6	0.52
B	2	0.054	0.005	0.002	0.4	0.65
C	2	0.041	0.057	0.028	5.0	0.01
Error	18	0.021	0.010	0.005		
Total	26	0.416				

Table 7. Response Table for Grey Relation Grade

Symbol	level 1	level 2	level 3	Main effect	Rank
A	0.5887	0.5541	0.3533	0.23541	2
B	0.4746	0.5457	0.6274	0.15274	3
C	0.7477	0.5338	0.4603	0.28739	1

Confirmation test is used to prove the accuracy of the developed model after identifying the optimal design. The experimental result which is having the high grade value using the initial arrangement of the cutting parameters is compared with the optimal one. Then the experiment is done with the new optimal design for MRR and SR and from Table 8, it is observed that the MRR increases from 7.65mm³/min to 1.31 mm³/min and SR decreases from 1.31µm to 1.28µm in the optimal combination of cutting parameters.

Table 8. Result of GRA Confirmation Test for MMC

Design	Output Parameters				
	Cutting speed	Feed	Depth of Cut	MRR (mm ³ /min)	SR (µm)
Initial Design	250	0.05	1.25	6.14	1.31
Optimal Design	250	0.06	1.5	7.65	1.28

5. Conclusion

In this work machining process is done by response surface methodology design of experiment. The optimal parameters were predicted by GRA technique. However these techniques concentrated on achieving a single quality characteristic at a time as a function of different appropriate levels of a number of input parameter settings. Improving one particular quality characteristic would possible lead to serious degradation of the quality characteristics. The optimal process parameter is predicted from GRA technique is 250m/min, 0.06mm, 1.5mm and responses are influencing process parameters.

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