Robust Diagnosis of Vehicular Active Suspension System Using Bond Graph Approach

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Abstract

Diagnostic systems play a major role in the safety of industrial systems and the availability of its equipment. Rapid detection (as soon as possible) to the operator of the detected deviations (defects) in relation to the expected nominal behavior is fundamental for the implementation of preventive and corrective actions on industrial systems.

These industrial systems are governed by several physical phenomena and various technological components, which is why the Bond Graph tool, based on an energy and multi-physical analysis, is well suited. In this article, we will discuss the problem of diagnosing an active suspension system of a vehicle by presenting diagnostic methods. Then, we introduce the bond graph tool for the robust diagnosis of the system. Finally, the extension of the deterministic models presented to models integrating uncertain elements (Fractional linear transformations LFT) and the generation of robust analytical redundancy relationships are also detailed.

Keywords: *Robust Diagnosis, Bond Graph, Vehicular Active Suspension System, Fractional Linear Transformations.*

1. Introduction

In an industrial system, the slightest failure is catastrophic in an environment where performance is paramount. For this, it is evident to ensure that the process is functioning properly in relation to the objectives that have been summoned to it [1-6].

The information to translate the behavior of a system is given by the measurements of the variables of it. Indeed, the quality of the measurements is an essential element to allow the system of diagnosis and the evaluation of the performances of a process. The quality of the information can be increased by improving the accuracy of the instrumentation and by multiplying the number of sensors. For technical or financial reasons, this solution is reserved for high-tech industries or those with high technological risks. Moreover, this hardware redundancy does not make it possible to protect against a failure of certain common elements of the measurement chain [7-12].

Moreover, analytical redundancy has the advantage of not increasing the cost of the installation and freeing itself from the hardware constraints. In the field of diagnostics, methods based on the concept of information redundancy have been developed. Their principle is generally based on a test of coherence between an observed behavior of the process provided by sensors and an expected behavior provided by a mathematical representation of the process.

Analytical redundancy methods therefore require a model of the system to be monitored. This model includes a number of parameters whose values are assumed to be known during normal operation. The comparison between the actual behavior of the system and the expected behavior given by the model provides a quantity called the residue that will be used to determine whether the system is in a failing state and to specify the part or component of the system faulty system [13-18].

Automation engineers consider the Bond Graph approach as the most reliable approach among other approaches to monitoring industrial plants. This reliability is given not only the modeling and the simulation but also the certain and uncertain diagnosis.

In this article, we are interested in the methods of certain and uncertain diagnosis based on the bond graph model. At the beginning, the definite approach is presented by the generation of the analytic redundancy relations using the leap graph approach. In the following, the extension of the deterministic models presented to models integrating uncertain elements (Linear Fractional Transformations LFT) and the generation of robust analytical redundancy relationships (ARRs) are also detailed in this paper. Finally, a general conclusion and perspectives are given [19-22].

This article is organized as follows:

▪ Section 2: The first part presents a reminder on the modelling of industrial systems by the bond graph approach; the second part is devoted to the robust diagnosis of industrial systems by the leap graph approach.

▪ Section 3: This section is devoted to the implementation of the proposed method on an active vehicle suspension system.

▪ Section 4: This section presents a conclusion of this work.

2. Robust Diagnosis by Bond Graph

2.1. Bond Graph Model

The Bond Graph model of a physical system explicates the power exchanges (symbolized by links) intervening between different elements (represented by nodes) that produce, dissipate, store or transmit energy. At each node of the Bond Graph is associated one or two characteristic relations of the physical phenomenon symbolized. We thus obtain directly a set of relations between the

magnitudes force and flux used to parameterize the physical system.

The notion of power is described by the following relation:

$$P(t) = \dot{e}(t).f(t) \tag{1}$$

This equation illustrates energy transfers in the system by using power bonds. A power link [23] is symbolized by a half arrow, whose orientation indicates the direction of power transfer. Thus, figure 1 shows the power transfer from subsystem S_1 to subsystem S_2.

Each power link carries two information's simultaneously: the effort and the flow (see figure 1). These are the generalized power variables (their product being the transferred power).
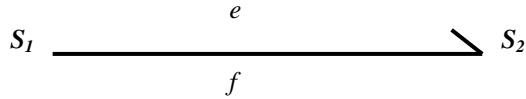

Fig.1: Power link

2.2. Fractional Linear Transformations Model

Fractional linear transformations (LFT) are generic objects widely used in the modeling of uncertain systems. The universality of fractional linear transformations is due to the fact that any rational expression can be written in this form [24-30]. This form of representation is widely used for the synthesis of control laws of uncertain systems using the principle of μ-analysis. It consists of separating the nominal part of a model from its uncertain part as shown in figure 2. The nominal values are grouped together in an augmented matrix denoted P, supposed to be proper, and the uncertainties whatever their type (structured and unstructured parametric uncertainties, modeling uncertainties, measurement noises, etc.) are combined in a matrix Δ of structure diagonal shown in figure 2.
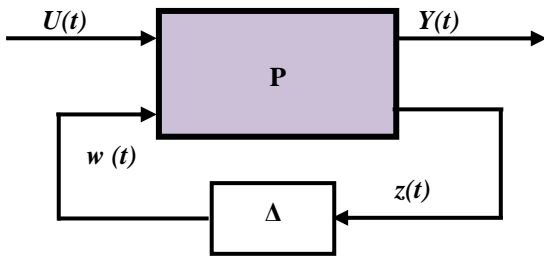

Fig. 2: Representation LFT

2.3. Construction of a Model BG-LFT

All industrial systems can be modeled by a hop graph model according to figure 3. Indeed, the input signal is modeled by a source of effort (*Se*) or a source of the flux (*Sf*), the whole system is Modeled by resistive elements (*R*) and storage elements (*I* or *C*) while the detectors are modeled by elements of the detectors (*De* or *Df*).
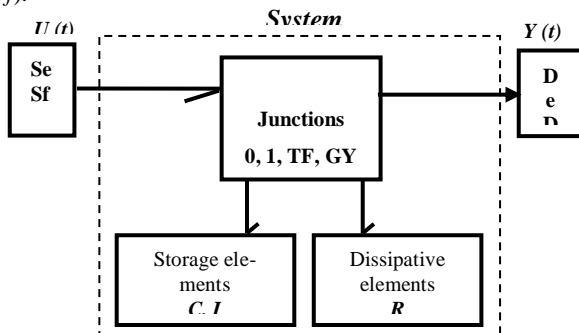

Fig. 3: Industrial system described by bond graph

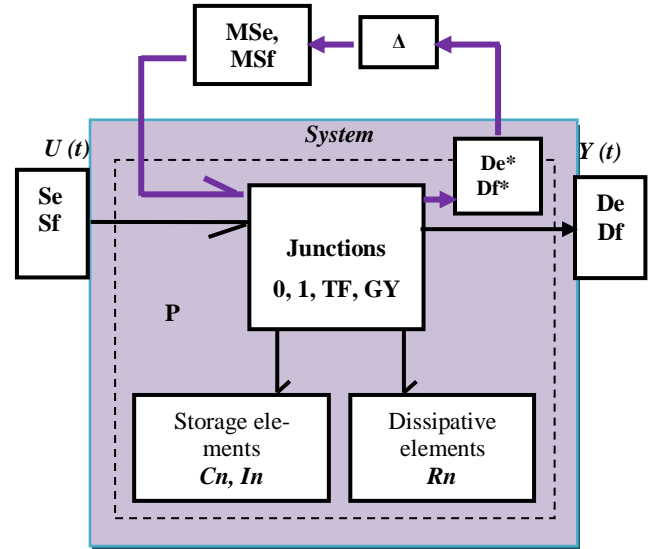Full BG-LFT can then be represented by the diagram in figure 4.

Fig. 4: Industrial system described by bond graph using LFT

2.3. Generate Robust Residuals

The generation of robust analytical redundancy relations from a clean bond graph model, observable and over determined is summarized by the following steps:

- *1st step*: Checking the status of the coupling on bond graph deterministic model derived preferential causality; if the system is over determined, then continue the following steps;
- *2nd step:* The bond graph model is made into LFT;
- *3rd step:* The symbolic expression of analytical redundancy relationships (ARRs) is inferred from equations junctions. This first form will be expressed by:

✓   For a junction 0:

$$\sum b_i f_{inc} + \sum \dot{S}f + \sum w_i \tag{2}$$

✓   For a junction 1:

$$\sum b_i e_{inc} + \sum \dot{S}e + \sum w_i \tag{3}$$

With the sum of sources flows due to the junction 0, the sum of the flow sources related to junction 1, b = ± 1 depending on whether the half-arrow into or out of the junction and e_{inc} and purpose are unknown variables.

- *4th step:* The unknown variables are eliminated by browsing the causal paths between sources and detectors or unknown variables;
- *5th step:* After removing the unknown variables, are uncertain as ARRs (5):

$$RRA : \Phi(\sum \dot{S}e, \sum Sf, De, Df, \tilde{D}e, \tilde{D}f,$$
$$\sum w_i, R_n, I_n, C_n, TF_n, GY_n) \tag{4}$$

Or:

- *TF_n* and *Gy_n* are nominal elements *TF* and *GY* ;
- *R_n*, *C_n* and *I_n* are nominal elements *R*, *C* and *I*;

- $\sum w_i$ is the sum of modulated inputs corresponding to uncertainties on the junction-related items**.**

3. Vehicular Active Suspension

Consider the vehicular active suspension system and its bond graph model given in figure 4.
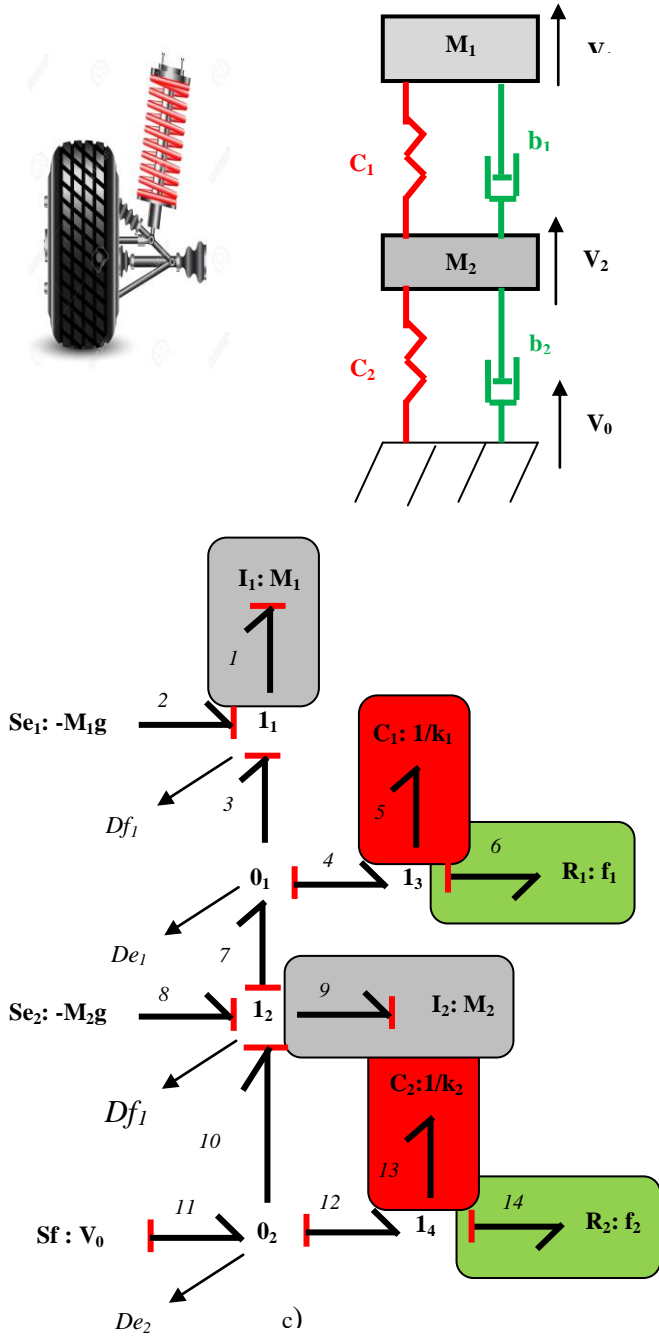

Fig. 5 : a) Real system vehicular active suspension, b) Mechanic model, c) Bond graph model

The vehicular active suspension system shown in the figure 5 b) is modeled by bond graph in figure 5 c) as follows:
- The mass of the vehicle frame is modeled by inertial element (*I: M_1*);
- The mass of the wheel is modeled by inertial element (*I: M_2*);
- The Shock of the vehicle is modeled by resistive element (*R: f_1*);
- The damping of the tire is modeled by resistive element (*R: f_2*);
- The spring rate of the vehicle is modeled by potential element (*C: $1/k_1$*);
- The spring rate of the tire is modeled by potential element (*C: $1/k_2$*);

3.1. Simulations of the Vehicular Active Suspension System

Figure 6 shows the evolution of the speed on the force exerted on the mass (*M*) and the forces exerted on the damping (k_1) and (k_2).
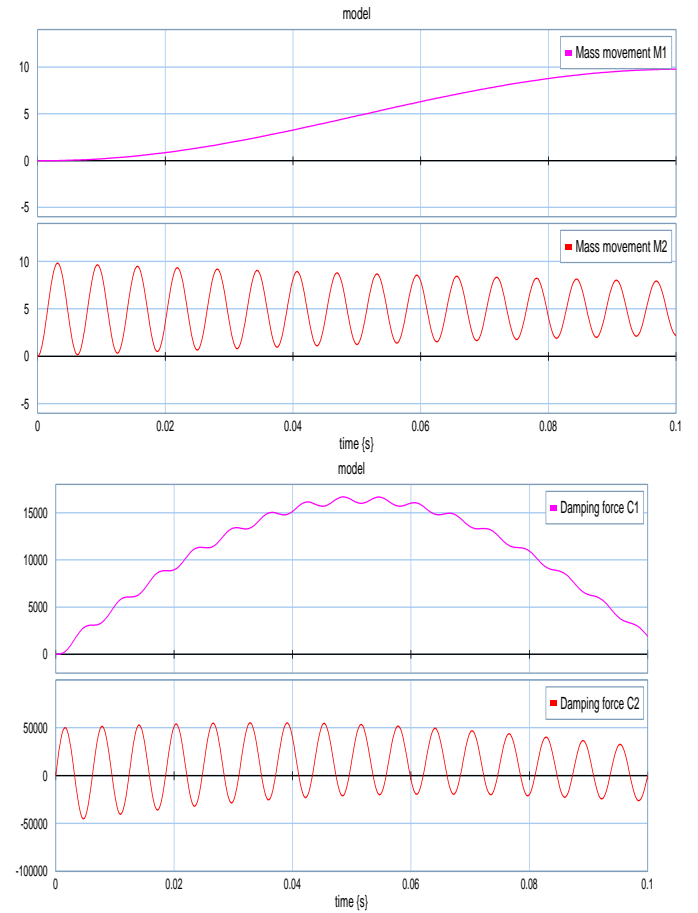

Fig. 6: a) Evolution of the speed on the masse (*M_1* and *M_2*), b) Evolution the Strengths of the damping (k_1 and k_2)

3.2. Determination of Residue Equations

- For example, the junction 1_1 gives us as equation:

$r_1 = e_1 - e_2 - e_3$

According to these relations, one can deduce the residual equation r_1:

$$r_1 = -M_1 \cdot g - M \frac{dDf_1}{dt} - De_1 \tag{6}$$

- The junction 0_1 gives us as equation:
$$r_2 = f_7 - f_3 - f_4$$

According to these relations, one can deduce the residual equation r_2:

$$r_2 = Df_2 - Df_1 - \frac{1}{f_1} De_1 - \frac{k_1}{f_1} \int Df_2 - Df_1 \tag{7}$$

- The junction 1_2 gives us as equation:

$r_3 = e_{10} - e_9 - e_8 - e_7$

According to these relations, one can deduce the residual equation r_3:

$$r_3 = De_2 - M_2 \cdot g - M_2 \frac{dDf_2}{dt} - De_1 \tag{8}$$

- The junction 0_2 gives us as equation:

$$r_4 = f_{11} - f_{10} - f_{12}$$

According to these relations, one can deduce the residual equation r_4:

$$r_4 = v - Df_2 - \frac{1}{f_2} De_2 - \frac{k_2}{f_2} \int v - Df_2 \qquad (9)$$

The rows of the fault signature matrix are associated with the set of residues r_1, r_2, r_3 and r_4 the columns with the variables of the possible faults Fj ($j =1, 2 ..., n$). $S_{ij} = 1$ (or 0), if the residue i sensitive (insensitive) to the fault j, we obtain the following signatures table 1:

Table 1: Fault Signatures Matrix for the Vehicular Active Suspension System

Element/Residue	r_1	r_2	r_3	r_4
Se$_1$: M$_1$.g	1	0	0	0
Se$_2$: M$_2$.g	0	0	1	0
C$_1$: 1/k$_1$	0	1	0	0
C$_2$: 1/k$_2$	0	0	0	1
R$_1$: f$_1$	0	1	0	0
R$_2$: f$_2$	0	0	0	1
I$_1$: M$_1$	1	0	0	0
I$_2$: M$_2$	0	0	1	0
Df$_1$	1	1	0	0
Df$_2$	0	1	1	1
De$_1$	1	1	0	0
De$_2$	0	0	1	1

Figure 7 shows the evolution of residues r_1, r_2, r_3 and r_4 as a normal function. The pitches of the residues converge towards zero under normal operating conditions
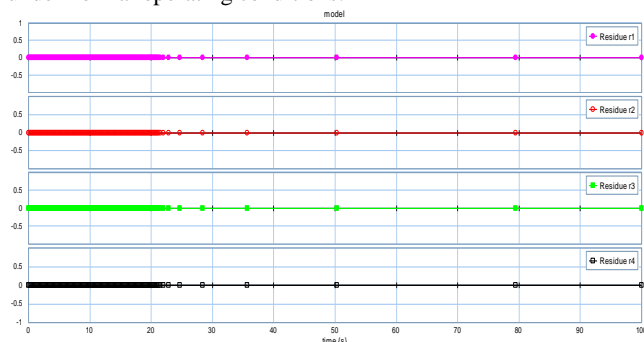
Fig.7: Evolution of residues r_1, r_2, r_3 and r_4 as a normal function

3.3. Simulation Active Suspension System with Fault

✓ fault on the damper (k_1)

Figure 8 show that, when a fault occurs on the damper k_1, the patterns of the residues r_1, r_2, r_3 and r_4 have non-zero average values, hence these residues are sensitive to this defect and this is confirmed by the theoretical results presented in table 1.
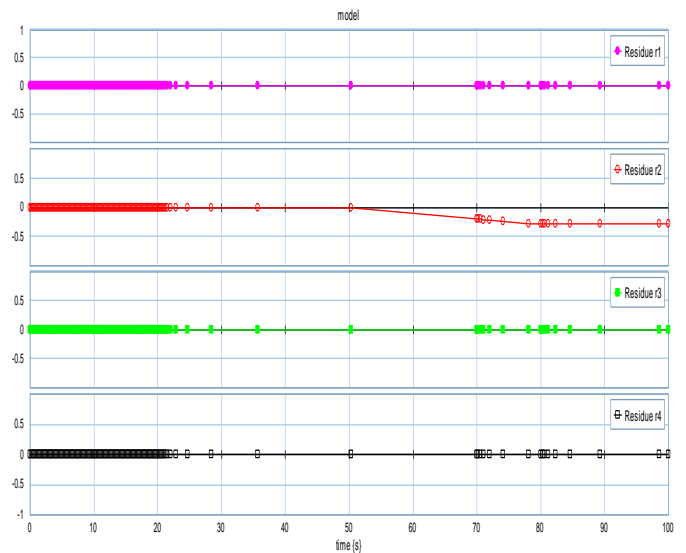
Fig.8: Evaluation of residues in the case of default in damper k_1

Figure 9 shows that when a defect occurs on the damper k_1, the variation of the forces exerted on the shock absorbers k_1 and k_2 varies at the same time.
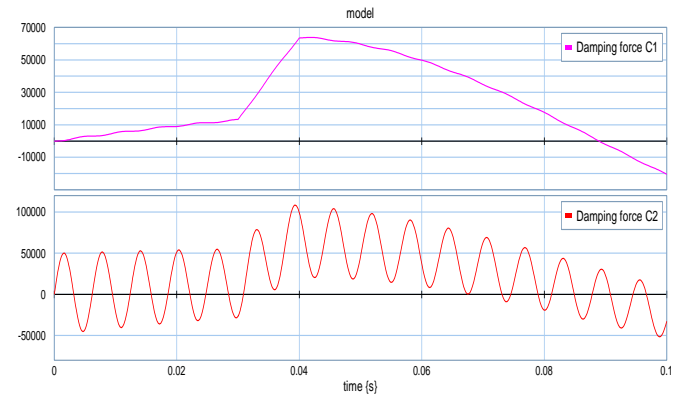
Fig. 9: Evolution of the speed on the masse and the Strengths of the damping (k_1) and (k_2) in the case of default in damper k_1

✓ fault on the damper (k_2)

Figure 10 show that, when a fault occurs on the damper k_2, the patterns of the residues r_1, r_2, r_3 and r_4 have non-zero average values, hence these residues are sensitive to this defect and this is confirmed by the theoretical results presented in table 1.
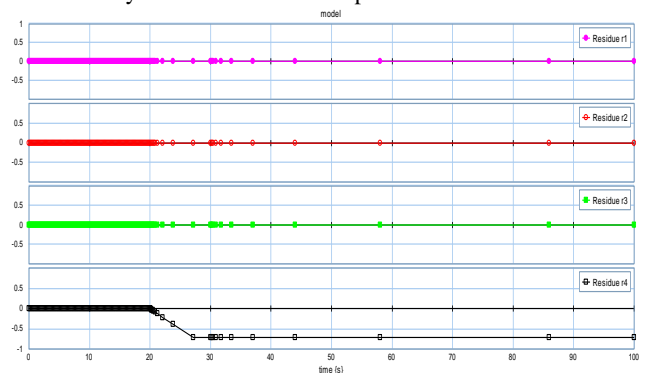
Fig.10: Evaluation of residues in the case of default in damper k_2

Figure 11 shows that when a defect occurs on the damper k_2, the change in the forces exerted on the dampers k_1 and k_2 varies at the same time.
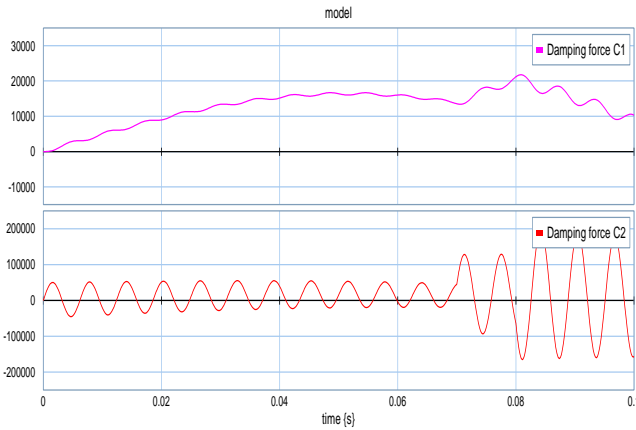
Fig. 11: Evolution of the speed on the masse and the Strengths of the damping (k_1) and (k_2) in the case of default in damper k_2

3.4. Robust diagnosis by bond graphs

Figure 12 shows the BG-LFT model of the hydraulic system.

■ For example, the junction 1_1 gives us as equation

$$R_{d1} = e_1 - e_2 - e_3 + Y_{s1}$$

According to these relations, one can deduce the residual equation R_1:

$$R_{d1} = \left[M_1 \cdot g \quad M_1 \frac{dSSf_1}{dt} \quad SSe_1 \right] + Y_{s1} + w_{M1} \tag{10}$$

The equation consists of two parts: the first part is the normal evolution of the residual r_{1n} and the second part represents the residual uncertainty related to the evolution of the parameters d_1:

$$R_{d1} = r_{1n} + d_1$$

$$r_{1n} = \left[M_1 \cdot g \quad M_1 \frac{dSSf_1}{dt} \quad SSe_1 \right]$$

$$d_1 = Y_{S1} + w_{M1}$$

■ The junction 0_1 gives us as equation:

$$R_{d2} = f_7 - f_3 - f_4$$

According to these relations, one can deduce the residual equation r_2:

$$R_{d2} = SSf_2 \quad SSf_1 \quad \frac{1}{f_1} SSe_1 \quad \frac{k_1}{f_1} \int SSf_2 \quad SSf_1 + w_{f1} + w_{\frac{1}{k1}} \tag{11}$$

The equation consists of two parts: the first part is the normal evolution of the residual r_{2n} and the second part represents the residual uncertainty related to the evolution of the parameters d_2:

$$R_{d2} = r_{2n} + d_2$$

$$r_{2n} = SSf_2 \quad SSf_1 \quad \frac{1}{f_1} SSe_1 \quad \frac{k_1}{f_1} \int SSf_2 \quad SSf_1$$

$$d_2 = w_{f1} + w_{\frac{1}{k1}}$$

■ The junction 1_2 gives us as equation:

$$R_{d3} = e_{10} - e_9 - e_8 - e_7$$

According to these relations, one can deduce the residual equation R_3:

$$R_{d3} = SSe_2 \quad M_2 \cdot g \quad M_2 \frac{dSSf_2}{dt} \quad SSe_1 + w_{M2} \tag{12}$$

The equation consists of two parts: the first part is the normal evolution of the residual r_{3n} and the second part represents the residual uncertainty related to the evolution of the parameters d_3:

$$R_{d3} = r_{3n} + d_3$$

$$r_{3n} = SSe_2 \quad M_2 \cdot g \quad M_2 \frac{dSSf_2}{dt} \quad SSe_1 + w_{M2}$$

$$d_3 = w_{M2}$$

■ The junction 0_2 gives us as equation:

$$R_{d4} = f_{11} - f_{10} - f_{12} + Y_{s2}$$

According to these relations, one can deduce the residual equation r_4:

$$R_{d4} = v \quad SSf_2 \quad \frac{1}{f_2} SSe_2 \quad \frac{k_2}{f_2} \int SSf_2 + Y_{s2} + w_{f2} + w_{\frac{1}{k2}} \tag{13}$$

The equation consists of two parts: the first part is the normal evolution of the residual r_{4n} and the second part represents the residual uncertainty related to the evolution of the parameters d_4:

$$R_{d4} = r_{4n} + d_4$$

$$r_{4n} = v \quad SSf_2 \quad \frac{1}{f_2} SSe_2 \quad \frac{k_2}{f_2} \int SSf_2$$

$$d_4 = Y_{s2} + w_{f2} + w_{\frac{1}{k2}}$$

4. Conclusion

The choice of the LFT form for the modeling of parametric uncertainties with the hop graphs on a nano-technology system made it possible to use a single tool for the systematic generation of indicators of formal uncertainty. These parametric uncertainties are explicitly introduced on the physical model thanks to its graphic architecture, which makes it possible to clearly show on the model their origins.

From a theoretical point of view, the uncertain analytical redundant relations (ARRs) generated are well structured, showing separately the energy contribution of the uncertainties to the default indicators and facilitating their evaluations in the decision step. From a practical point of view, the fields of application of this method are very vast thanks to the energy and multi-physical aspect of the bond graphs, and to the LFT form used to model the influence of the uncertainties on the system. The developed procedure is implemented on a 20SIM software tool [27].
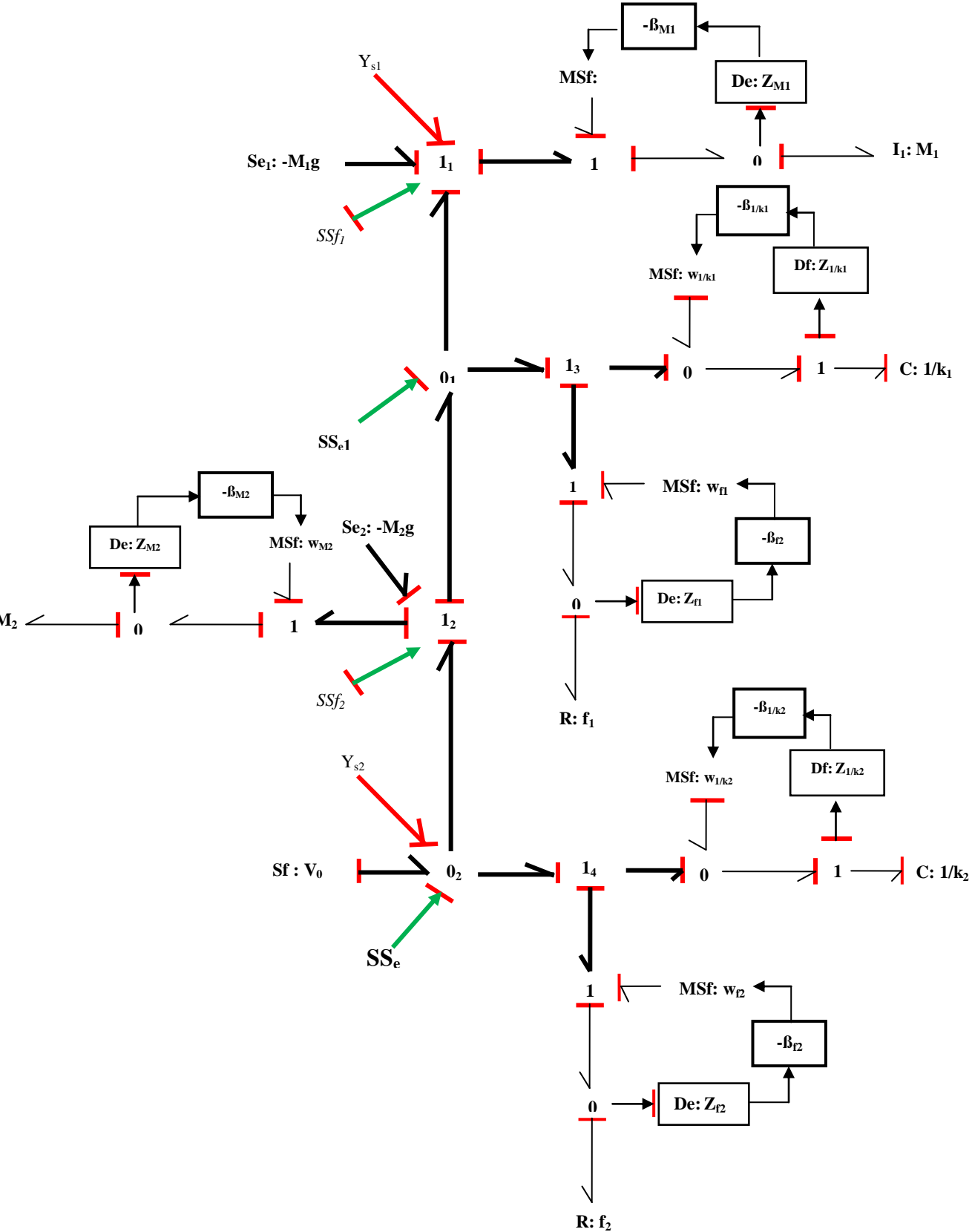
Fig.12: BG-LFT model of the hydraulic system

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Acknowledgment

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